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Peter V. Danchev

EFI $p^{\omega+3}$ -PROJECTIVE Σ -GROUPS ARE NOT NECESSARILY
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Abstract: We extend an example due to Cutler-Missel (Comm. Alg., 1984) of a separable efi $p^{\omega+2}$ -projective abelian p -group which is not C-decomposable and thick by showing that there exists even an inseparable efi $p^{\omega+3}$ -projective p -torsion Σ -group which is neither C-decomposable nor thick. This supplies two recent results of ours in (Comm. Alg., 2008).

Cihan Özgür

ON GENERALIZED RECURRENT CONTACT METRIC MANIFOLDS 11-19

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A. Boccuto, B. Riečan and A. R. Sambucini

SOME PROPERTIES OF AN IMPROPER GH_k INTEGRAL IN
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Abstract: We investigate the GH_k integral for functions defined on (possibly) unbounded subintervals of the extended real line and with values in Riesz spaces. Some convergence theorems are proved, together with a version of the Fundamental Formula of Calculus.

A. A. Shaikh, Y. Matsuyama and Sanjib Kumar Jana

ON A TYPE OF GENERAL RELATIVISTIC SPACETIME WITH
 W_2 -CURVATURE TENSOR

53-62

Abstract: Most of the matter in the universe can, in some form or other, be treated as a fluid and in several phenomena such as supernova explosions, jets in extragalactic radio sources, accretions onto neutron stars and black holes, high-energy particle beams, high-energy nuclear collisions etc. undergoes the relativistic motion. In the general relativity the matter content of the spacetime is described by the energy-momentum tensor which is determined from physical considerations dealing with the distribution of the matter and energy. Since the matter content of the universe is assumed to behave like a perfect fluid in the standard cosmological model, the physical motivation for studying Lorentzian manifolds is the assumption that a gravitational field may be effectively modelled by some Lorentzian metric defined on a suitable four dimensional manifold which is called the general relativistic spacetime. The object of the present paper is to study a type of a general relativistic spacetime with vanishing and as well as the divergence free W_2 -curvature tensor.

Eduard V. Musafirov

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Zhengxin Zhou

THE QUALITATIVE BEHAVIOUR OF NONLINEAR DEFFERENTIAL
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77-86

Abstract: In this paper, we give some criteria for the nonlinear differential systems to be simple systems and find out their reflective functions. The results are applied to the discussion of the behavior of solutions of these nonlinear differential systems. In particular, we discuss the qualitative behavior of solutions of Riccati equation.

Xiaolong Qin, Meijuan Shang and Yongfu Su

(A, η) -RESOLVENT OPERATOR TECHNIQUE FOR GENERALIZED
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Ian Twedde

A CLASS OF TOPOLOGIES ON THE SPACE OF BOUNDED
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P. N. Natarajan and S. Sakthivel

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Abstract: In the present paper, K denotes a complete, non-trivially valued, non-archimedean field. Entries of sequences, series and infinite matrices are in K . The purpose of the present paper is to extend Theorem 1 of [2] for double series, introduce the concept of convolution for double infinite matrices and to prove some basic results related to that concept in non-archimedean fields.

Bruno Scardua

ON THE CLASSIFICATION OF C^n -ACTIONS AND STEIN
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states that a Stein manifold M of dimension $n + 1$ and equipped with a holomorphic action of the complex additive group \mathbb{C}^n such that the corresponding foliation has a suitable dicritical singularity is biholomorphic to \mathbb{C}^{n+1} . Indeed, there is a partial linearization for the action on M .

Biljana Krsteska and Erdal Ekici

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Abstract: The concept of fuzzy contra strongly precontinuous mapping are introduced and studied. Properties and relationship of fuzzy contra strongly precontinuous mapping are established. Also, some applications to fuzzy compact spaces are given.

Jionghui Cai, Shaolong Xie and Wen Qiu

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Songxio Li and Stevo Stević

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Abstract: Let $g : B \rightarrow \mathbb{C}^1$ be a holomorphic map on the unit ball B . This note studies the boundedness and compactness of the

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$$T_g f(z) = \int_0^1 f(tz) \Re g(tz) \frac{dt}{t} \quad \text{and} \quad L_g f(z) = \int_0^1 \Re f(tz) g(tz) \frac{dt}{t},$$

$z \in B$, between different mixed norm spaces of holomorphic functions $H_{p_1, q_1, \gamma_1}(B)$ and $H_{p_2, q_2, \gamma_2}(B)$.

Motohico Mulase and Brad Safnuk

MIRZAKHANI'S RECURSION RELATIONS, VIRASORO

CONSTRAINTS AND THE KdV HIERARCHY

189-218

Abstract: We present in this paper a differential version of Mirzakhani's recursion relation for the Weil-Petersson volumes of the moduli spaces of bordered Riemann surfaces. We discover that the differential relation, which is equivalent to the original integral formula of Mirzakhani, is a Virasoro constraint condition on a generating function for these volumes. We also show that the generating function for ψ and κ_1 intersections on $\overline{M}_{g,n}$ is a 1-parameter solution to the KdV hierarchy. It recovers the Witten-Kontsevich generating function when the parameter is set to be 0.

Ishak Altun and Duran Turkoglu

A FIXED POINT THEOREM ON GENERAL TOPOLOGICAL

SPACES WITH A τ -DISTANCE

219-228

Abstract: In this paper, we prove some fixed point theorem for mappings satisfying contractive condition of integral type on general topological spaces using a τ -distance which is given by Aamri and El Moutawakil in [1]. Our results extend and generalize the results of Aamri and El Moutawakil [1], Branciari [4] and some others.

S. L. Singh and Rajendra Pant

COINCIDENCES AND FIXED POINTS OF NON-CONTINUOUS

MAPS

229-237

Abstract: The main purpose of this paper is to obtain coincidence and common fixed point theorems for non-continuous maps using (IT)-commutativity. Some recent results are improved considerably.