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**Abstract:** In this paper, we extend celebrated fixed point theorems of Boyd-Wong and Matkowski from the class of continuous mappings to a wider class of mappings which also include discontinuous mappings at the fixed point. As a by-product, we provide a new solution to the open problem on the existence of a contractive mapping which has a fixed point but is discontinuous at the fixed point (see Rhoades [Contractive definitions and continuity, Contemporary Mathematics 72(1988), 233-245], p. 242).

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**Abstract:** As a generalization of the Schwarzschild solution, Vaidya presented a radiating metric to develop a model of the exterior of a star including its radiation field, named later Vaidya metric. The present paper deals with the investigation on the curvature properties of Vaidya metric. It is shown that Vaidya metric can be considered as a model of different pseudosymmetric type curvature conditions, namely,  $C \cdot C = \frac{m}{r^3} Q(g, C)$ ,  $R \cdot R - Q(S, R) = \frac{m}{r^3} Q(g, C)$ , etc. It is also shown that Vaidya metric is Ricci simple, vanishing scalar curvature and its Ricci tensor is Riemann-compatible. As a special case of the main result, we obtain the curvature properties of Schwarzschild metric. Finally,

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